

MATH 42-NUMBER THEORY  
PROBLEM OF THE DAY #8  
DUE THURSDAY, MARCH 3, 2011

1. Using linear diophantine equations, find  $a$  that satisfies the following.

$$a \equiv 0 \pmod{5}$$

$$a \equiv 0 \pmod{7}$$

$$a \equiv 1 \pmod{22}$$

Find  $b$  that satisfies

$$b \equiv 0 \pmod{5}$$

$$b \equiv 1 \pmod{7}$$

$$b \equiv 0 \pmod{22}$$

and  $c$  that satisfies

$$c \equiv 1 \pmod{5}$$

$$c \equiv 0 \pmod{7}$$

$$c \equiv 0 \pmod{22}$$

Use  $a, b, c$  to find  $x$  that satisfies

$$x \equiv 1 \pmod{5}$$

$$x \equiv 2 \pmod{7}$$

$$x \equiv 3 \pmod{22}$$